

## Delay-Insensitive Variable-Rate Selective Excitation (DIVERSE)

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**Purpose:** Variable-rate selective excitation<sup>1,2</sup> (VERSE) is a powerful technique that allows RF pulse designers to vary the selective excitation gradient to reduce peak  $B_1$  and SAR. While the profile dependence on off-resonance for VERSE pulses has been previously discussed<sup>1</sup>, this work concentrates on the profile dependence on gradient-RF system delay, showing there is high sensitivity to this delay. We further present a novel design method, time-optimal delay-insensitive variable-rate selective excitation (DIVERSE), which shows improved robustness to gradient-RF system delay.

**Methods:** The contribution to the final transverse magnetization  $M_{xy}(z, t)$  at time  $T$  from the segment  $[t, t+dt]$  of an RF pulse  $B_1(t)$  of duration  $T$  in the presence of a time-varying gradient  $G_z(t)$  can be approximated in the small-tip-angle regime as:

$$M_{xy}(z, t) = iM_0\gamma B_1(t)dt \cdot e^{izk_z(t)}, \quad \text{where } k_z(t) = -\gamma \int_t^T G_z(s)ds$$

If we assume a delay  $\delta$  between the gradient and RF, caused either by system delays or eddy current effects, then the magnetization  $M_{xy,\delta}(z, t)$  will be given by:

$$M_{xy,\delta}(z, t) = iM_0\gamma B_1(t)dt \cdot e^{izk_z(t+\delta)}.$$

The difference  $|M_{xy,\delta}(z, t) - M_{xy}(z, t)|$  can be simplified using a Taylor series expansion for  $k_z(t+\delta) \approx k_z(t) + \partial k_z(t) = k_z(t) - \gamma\delta G_z(t)$  to:

$$|M_{xy,\delta}(z, t) - M_{xy}(z, t)| \propto |B_1(t)| \cdot |zG_z(t)|. \quad [1]$$

As a consequence of [1], we introduce an additional constraint on VERSE'd gradient and RF waveforms for DIVERSE pulses such that  $|B_{1,v}(t)| \cdot |G_{z,v}(t)| \leq K_{dv} B_{1,max} G_{max}$ , where  $K_{dv}$  is  $\leq 1$ ; and  $B_{1,max}$  and  $G_{max}$  are the system limits. Introducing this term as an additional gradient constraint in the arc-length-based time-optimal VERSE approach<sup>3</sup> ensures time-optimality of the DIVERSE pulses. A DIVERSE pulse with  $K_{dv}=1$  is equal to a minimum-time VERSE (MT-VERSE) pulse<sup>3</sup>.

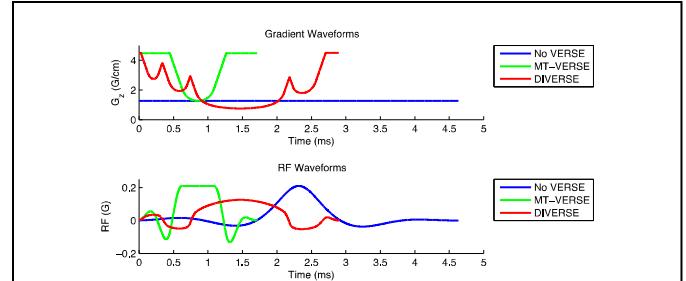
**Results:** Figure 1 shows VERSE designs of a spin-echo pulse with system limits of  $B_{1,max} < 0.21\text{G}$ ,  $G_{max} < 4.5\text{G/cm}$ , and  $S_{max} < 14\text{G/cm/ms}$ . The DIVERSE design with  $K_{dv}=10\%$  reduces the RF pulse duration to 62% that of the non-VERSE 4.6-ms pulse. The relative duration for the DIVERSE pulse can be reduced to 47% by setting  $K_{dv}=20\%$ , while the MT-VERSE relative pulse duration is only 37%.

Figure 2 illustrates the Bloch-simulated slice profile dependence on gradient-RF delay for the 10% DIVERSE and MT-VERSE pulses. The MT-VERSE pulse shows substantial sensitivity to delay when the RF pulse is modulated to offset the slice 6 cm from isocenter, while the DIVERSE pulse is much more robust. Figure 3 validates the simulations with experimental slice profiles acquired on a GE Discovery MR750 when a 4 $\mu\text{s}$  delay is intentionally introduced in the gradient-RF timing.

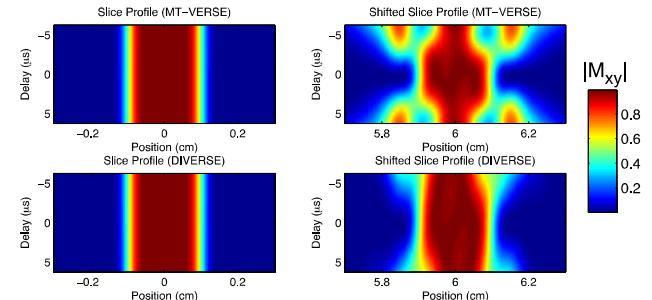
Figure 4 shows the  $T_2$  ( $b_0$ ) phantom images acquired 6 cm off isocenter with a diffusion-weighted EPI sequence using a single refocusing pulse. An intentional 4 $\mu\text{s}$  delay was introduced in the gradient-RF timing. The 10% DIVERSE image shows improved signal level and a sharper slice profile as expected.

**Discussion and Conclusions:** A novel approach for VERSE pulse design is presented that reduces sensitivity to gradient-RF delays. The constraint parameter  $K_{dv}$  can be adjusted to tradeoff reduction in pulse duration versus insensitivity to gradient-RF delay. Future work will evaluate DIVERSE pulses in simultaneous multislice DW-EPI sequences<sup>4</sup> where there is a need to reduce the duration of high peak  $B_1$  multislice spin-echo pulses.

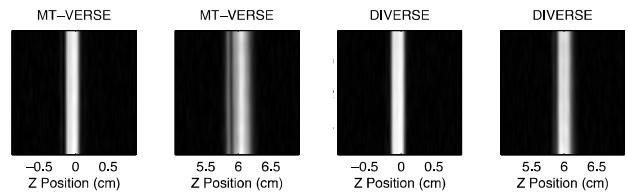
**References:** [1] Conolly *et al.*, JMR, 78(3):440–458, 1988. [2] Hargreaves *et al.*, MRM, 52(3):590–7, 2004. [3] Lee D *et al.*, MRM, 61(6):1471–9, 2009. [4] Setsompop *et al.*, MRM, 67(5):1210–24, 2012. [This work partly supported by NIH R01 EB008108, NIH R01 EB009756, NIH P41 EB015891.]



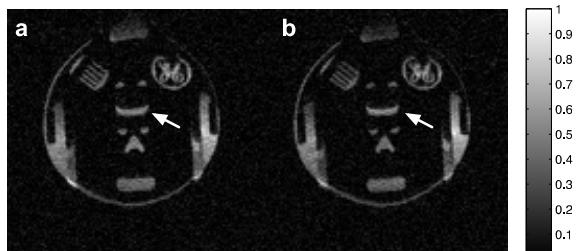
**Figure 1:** Gradient and RF waveforms for a refocusing pulse (time-bandwidth=5, 2-mm slice thickness) without VERSE (blue), and corresponding minimum-time VERSE (green) and DIVERSE (red) pulses with limit  $|B_{1,v}(t)| \cdot |G_{z,v}(t)| \leq 10\% B_{1,max} \cdot G_{max}$ .



**Figure 2:** Simulated slice profile  $|M_{xy}(z)|$  dependence on gradient-RF delay for the MT-VERSE and 10% DIVERSE pulses.



**Figure 3:** Experimental slice profiles for the MT-VERSE and 10% DIVERSE pulses at 0cm and 6cm from isocenter with an intentional 4 $\mu\text{s}$  gradient-RF delay introduced.



**Figure 4:**  $T_2$  ( $b_0$ ) images acquired 6 cm off isocenter with a diffusion-weighted EPI sequence using a single refocusing pulse that is the a) MT-VERSE or b) 10% DIVERSE pulse. The DIVERSE image shows 9% greater average signal and has improved slice sharpness as shown by the slice profile indicator of the phantom (arrow).