

Delay-Insensitive Variable-Rate Selective Excitation (DIVERSE)

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Purpose: Variable-rate selective excitation^{1,2} (VERSE) is a powerful technique that allows RF pulse designers to vary the selective excitation gradient to reduce peak B₁ and SAR. While the profile dependence on off-resonance for VERSE pulses has been previously discussed¹, this work concentrates on the profile dependence on gradient-RF system delay, showing there is high sensitivity to this delay. We further present a novel design method, time-optimal delay-insensitive variable-rate selective excitation (DIVERSE), which shows improved robustness to gradient-RF system delay.

Methods: The contribution to the final transverse magnetization $M_{xy}(z, t)$ at time T from the segment $[t, t+dt]$ of an RF pulse $B_1(t)$ of duration T in the presence of a time-varying gradient $G_z(t)$ can be approximated in the small-tip-angle regime as:

$$M_{xy}(z, t) = iM_0\gamma B_1(t)dt \cdot e^{ik_z(z, t)}, \quad \text{where } k_z(t) = -\gamma \int_t^T G_z(s)ds$$

If we assume a delay δ between the gradient and RF, caused either by system delays or eddy current effects, then the magnetization $M_{xy,\delta}(z, t)$ will be given by:

$$M_{xy,\delta}(z, t) = iM_0\gamma B_1(t)dt \cdot e^{ik_z(z, t+\delta)}.$$

The difference $|M_{xy,\delta}(z, t) - M_{xy}(z, t)|$ can be simplified using a Taylor series expansion for $k_z(t+\delta) \approx k_z(t) + \partial k_z'(t) = k_z(t) - \gamma \partial G_z(t)$ to:

$$|M_{xy,\delta}(z, t) - M_{xy}(z, t)| \propto |B_1(t)| \cdot |zG_z'(t)|. \quad [1]$$

As a consequence of [1], we introduce an additional constraint on VERSE'd gradient and RF waveforms for DIVERSE pulses such that $|B_{1,v}(t)| \cdot |G_{z,v}(t)| \leq K_{dv} B_{1,max} G_{max}$, where K_{dv} is ≤ 1 ; and $B_{1,max}$ and G_{max} are the system limits. Introducing this term as an additional gradient constraint in the arc-length-based time-optimal VERSE approach³ ensures time-optimality of the DIVERSE pulses. A DIVERSE pulse with $K_{dv}=1$ is equal to a minimum-time VERSE (MT-VERSE) pulse³.

Results: Figure 1 shows VERSE designs of a spin-echo pulse with system limits of $B_{1,max} < 0.21G$, $G_{max} < 4.5G/cm$, and $S_{max} < 14G/cm/ms$. The DIVERSE design with $K_{dv}=10\%$ reduces the RF pulse duration to 62% that of the non-VERSE 4.6-ms pulse. The relative duration for the DIVERSE pulse can be reduced to 47% by setting $K_{dv}=20\%$, while the MT-VERSE relative pulse duration is only 37%.

Figure 2 illustrates the Bloch-simulated slice profile dependence on gradient-RF delay for the 10% DIVERSE and MT-VERSE pulses. The MT-VERSE pulse shows substantial sensitivity to delay when the RF pulse is modulated to offset the slice 6 cm from isocenter, while the DIVERSE pulse is much more robust. Figure 3 validates the simulations with experimental slice profiles acquired on a GE Discovery MR750 when a 4 μ s delay is intentionally introduced in the gradient-RF timing.

Figure 4 shows the T₂ (b₀) phantom images acquired 6 cm off isocenter with a diffusion-weighted EPI sequence using a single refocusing pulse. An intentional 4 μ s delay was introduced in the gradient-RF timing. The 10% DIVERSE image shows improved signal level and a sharper slice profile as expected.

Discussion and Conclusions: A novel approach for VERSE pulse design is presented that reduces sensitivity to gradient-RF delays. The constraint parameter K_{dv} can be adjusted to tradeoff reduction in pulse duration versus insensitivity to gradient-RF delay. Future work will evaluate DIVERSE pulses in simultaneous multislice DW-EPI sequences⁴ where there is a need to reduce the duration of high peak B₁ multislice spin-echo pulses.

References: [1] Conolly *et al.*, JMR, 78(3):440–458, 1988. [2] Hargreaves *et al.*, MRM, 52(3):590–7, 2004. [3] Lee D *et al.*, MRM, 61(6):1471–9, 2009. [4] Setsompop *et al.*, MRM, 67(5):1210–24, 2012. [This work partly supported by NIH R01 EB008108, NIH R01 EB009756, NIH P41 EB015891.]

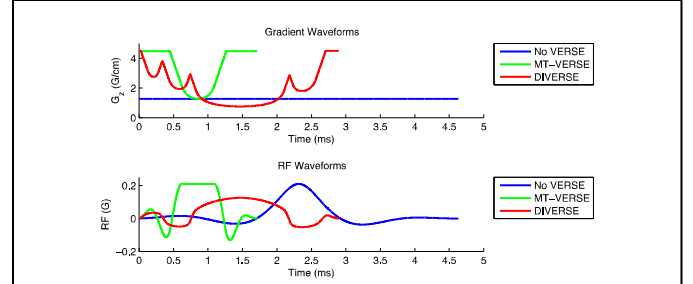


Figure 1: Gradient and RF waveforms for a refocusing pulse (time-bandwidth=5, 2-mm slice thickness) without VERSE (blue), and corresponding minimum-time VERSE (green) and DIVERSE (red) pulses with limit $|B_{1,v}(t)| \cdot |G_{z,v}(t)| \leq 10\% B_{1,max} \cdot G_{max}$.

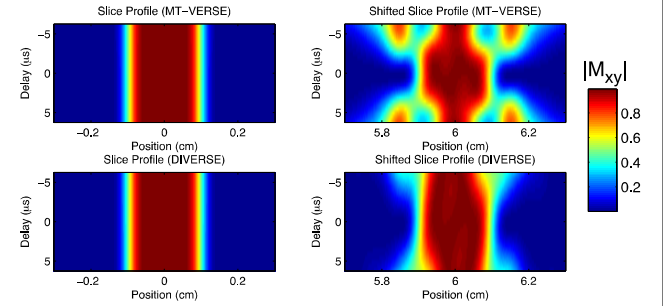


Figure 2: Simulated slice profile $|M_{xy}(z)|$ dependence on gradient-RF delay for the MT-VERSE and 10% DIVERSE pulses.

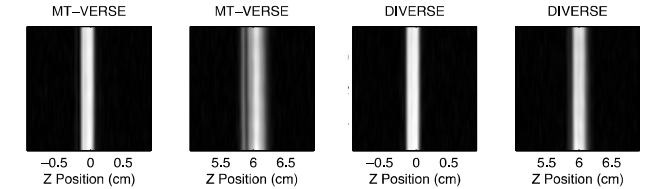


Figure 3: Experimental slice profiles for the MT-VERSE and 10% DIVERSE pulses at 0cm and 6cm from isocenter with an intentional 4 μ s gradient-RF delay introduced.

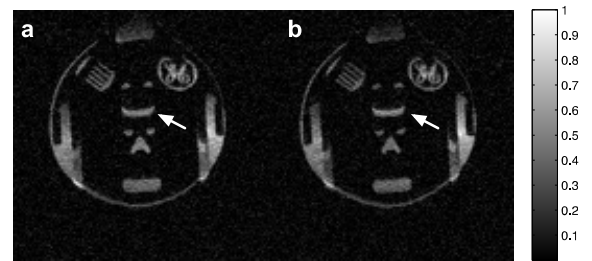


Figure 4: T₂ (b₀) images acquired 6 cm off isocenter with a diffusion-weighted EPI sequence using a single refocusing pulse that is the a) MT-VERSE or b) 10% DIVERSE pulse. The DIVERSE image shows 9% greater average signal and has improved slice sharpness as shown by the slice profile indicator of the phantom (arrow).