

## Optimisation of b-value distribution in biexponential modelling

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**Introduction** Traditionally, ADC determination involves mono-exponential fitting of diffusion weighted imaging (DWI) data, thus potentially ignoring microperfusion contributions to the signal decay at low  $b$ -values. Recent work has demonstrated that it is technically possible to acquire DWI data of the brain [1] and other organs [2-6] with low  $b$ -values in an attempt to quantify this perfusive fraction of the ADC decay curve via bi-exponential modelling. However, large uncertainties in the fitted parameters have prevented the widespread adoption of this technique. Efforts to optimise the acquisition protocol have been made [7] and it appears evident that increased sampling at low  $b$ -values to adequately define the rapidly decaying perfusive weighted component is necessary. Adapting the work of Shrager *et al* [8], which investigated optimal time spacing for  $T_2$  measurements in mono- and bi-exponential systems, this study aims to assess the optimal  $b$ -value spacing in bi-exponential modelling of various tissue organs.

**Methods** Synthetic data simulating the MR signal decay of a bi-exponential system was created in Matlab (The MathWorks Inc) using the following equation

$$S_b = S_0([1 - f]e^{-bD'} + fe^{-bD^*})$$

where  $f$  is the perfusion fraction,  $D'$  is the pure diffusion coefficient,  $D^*$  is the pseudo diffusion coefficient,  $b$  is the  $b$ -value, and  $S_0$  ( $S_b$ ) is the signal at a  $b$ -value of 0 ( $b$ ) s/mm<sup>2</sup>. Data was created for 4 tissue types using literature obtained parameter values (brain:  $f=5\%$ ,  $D^*=10\mu\text{m}^2/\text{ms}$ ,  $D'=1\mu\text{m}^2/\text{ms}$  [1]; breast:  $f=10\%$ ,  $D^*=15\mu\text{m}^2/\text{ms}$ ,  $D'=1.15\mu\text{m}^2/\text{ms}$  [2]; kidney:  $f=30\%$ ,  $D^*=15\mu\text{m}^2/\text{ms}$ ,  $D'=1.5\mu\text{m}^2/\text{ms}$  [3]; liver:  $f=30\%$ ,  $D^*=60\mu\text{m}^2/\text{ms}$ ,  $D'=1\mu\text{m}^2/\text{ms}$  [4]). Gaussian noise was added to produce data ranging from SNR=10:1 to SNR=1000:1. The simulated data was calculated using 10  $b$ -values determined from the Power Law formula where the  $i^{\text{th}}$   $b$ -value is given by

$$b_i = b_{\min} + (b_{\max} - b_{\min}) \left( \frac{i - 1}{n - 1} \right)^r$$

where  $b_{\min}=0$ ,  $b_{\max}=1000$  s/mm<sup>2</sup>,  $n=10$ , and  $r$  varied from 1 (linear spacing) to 5. For each combination of  $b$ -value distribution, organ parameters and SNR level 1000 cases were generated. Bi-exponential fitting was performed using simplex minimisation. Initial  $D'$  estimates were determined by a mono-exponential fit to  $b>500$  s/mm<sup>2</sup> data points with initial  $D^*$  and  $f$  estimates based on extrapolation of this mono-exponential curve to  $b=0$  s/mm<sup>2</sup>. Data was also fitted to a mono-exponential model for comparison.

**Results** For the brain data bi-exponential fitting consistently overestimated the perfusion fraction  $f$  in all but the highest SNR regimes with estimates of  $\sim 9.5\%$  at SNR < 20 compared with the nominal value of 5%. Mono-exponential analysis also provided a better fit (lower RMSE) in the low SNR regime. Similar results were obtained for breast synthetic data. For tissues with a high perfusion fraction (liver and kidney) bi-exponential fitting consistently outperformed mono-exponential fitting for all SNR values. Because of the rapid loss in signal from the perfusive component the optimal sampling strategy occurred when  $r=3.0$  (corresponding to  $b = 0, 1.4, 11, 37, 87, 171, 296, 471, 702$  and  $1000$  s/mm<sup>2</sup>) and above.

**Discussion** This work has demonstrated that bi-exponential fitting of synthetic DWI data is feasible using 10  $b$ -values. When a relatively small perfusive component fraction is present ( $\leq 10\%$ ) a relatively high SNR in the DW images appears to be necessary, otherwise a mono-exponential model provides a better fit. For tissues with a rapid ( $\geq 15\mu\text{m}^2/\text{ms}$ ) and large perfusive component ( $\geq 30\%$ ) adequate sampling of low  $b$ -values using a non-linear spacing strategy is paramount for accurate fitting. However, the use of very low  $b$ -values in imaging is often difficult, wherein imaging gradients may contribute significantly to the 'true'  $b$ -value as compared to the inputted desired  $b$ -value. Future work will attempt to assess the effect of imaging gradient contributions on the fitting methods developed.

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