## Analysis of the Transient Phase of Balanced SSFP with Non-continuous RF for Cardiac Imaging

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Introduction The transient phase of balanced SSFP (bSSFP) is the period during which magnetization approaches steady state. The transient phase of non-ECG-gated, continuous-RF bSSFP has been characterized by a simple exponential decay with a time constant that is a flip-angle-weighted average of  $T_1$  and  $T_2$  (1). Cardiac imaging applications, however, often utilize bSSFP with non-continuous RF excitation where bSSFP data is collected only during a short period of the cardiac cycle. For example, a Look-Locker-based cardiac  $T_1$  mapping sequence (Fig. 1) begins with an ECG trigger, and is followed by magnetization preparation (on the first cardiac cycle only), a bSSFP imaging segment, and a recovery time  $T_{rec}$  prior to the subsequent imaging segment. Multiple time points (i.e., inversion times, TI) are acquired, separated by the R-R interval  $T_{RR}$ . Another example, magnetization-prepared bSSFP, would utilize a preparation pulse and TI for each cardiac cycle. In this case,  $T_{rec}$  would be the time between the end of the bSSFP acquisition and the next preparation pulse. The continuous-RF transient phase as described in reference 1 is not applicable in these cases.

<u>Purpose</u> The goal of this work was to develop an analytical expression for the transient phase of bSSFP with non-continuous RF excitation. The resulting equation can be applied to Look-Locker acquisitions to provide true quantification of  $T_1$  (and  $T_2$ ), rather than an "apparent"  $T_1$  ( $T_1$ \*) for cardiac imaging.

**Methods** The Look-Locker pulse sequence is shown in Figure 1 and is periodic (after the initial preparation pulse). It begins with a data acquisition segment (with N views per segment) and ends with a recovery time  $T_{rec} = T_{RR} - N \times TR$  before the next segment. Let  $\mathbf{M}_T(n)$  be the transient magnetization at time point n (2). Assume that the magnetization at the subsequent time point  $\mathbf{M}_T(n+1)$  is a scaled version of  $\mathbf{M}_T(n)$ ; i.e,  $\lambda \mathbf{M}_T(n)$  (1). The transient response may then be written as

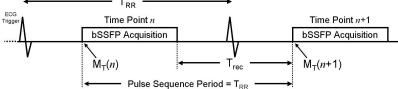


Figure 1. Pulse sequence diagram.  $M_T(n)$  is the transient magnetization prior to data acquisition at time point n. Magnetization preparation pulses may be played out between the ECG trigger and the bSSFP acquisition. For Look-Locker acquisitions, a preparation pulse is played out only during the first cardiac cycle of each Look-Locker experiment. For magnetization-prepared acquisitions, a preparation pulse is played out every cardiac cycle.

 $\mathbf{M}_{\mathrm{T}}(n+1) = \lambda \mathbf{M}_{\mathrm{T}}(n)$ . Because this resembles an eigenvalue equation, it may also be written as  $\mathbf{A}\mathbf{M}_{\mathrm{T}}(n) = \lambda \mathbf{M}_{\mathrm{T}}(n)$ . A is a transformation matrix that describes the change of the transient magnetization from segment to segment and can be derived from matrix modeling of one period of the pulse sequence. This work will show that the transformation matrix can be expressed as

$$\mathbf{A} = \mathbf{E}(T_{rec}) \left[ \mathbf{R}_z(\pi) \mathbf{E}(TR) \mathbf{R}_x(\alpha) \right]^N \prod_{i=M}^1 \mathbf{R}_z(\varphi_i) \mathbf{E}(\tau_i) \mathbf{R}_x(\alpha_i)$$

where  $\mathbf{R}_x$  and  $\mathbf{R}_z$  are rotation matrices for RF excitation and phase modulation, respectively;  $\mathbf{E}(t)$  represents relaxation during time t; and the product term ( $\Pi$ ) denotes steady-state preparation using any series of M pulses. The equation  $\mathbf{A}\mathbf{M}_T(n) = \lambda \mathbf{M}_T(n)$  can be solved for the real positive eigenvalue  $\lambda_{eig}$  of  $\mathbf{A}$ , which is a function of  $T_1$ ,  $T_2$ , and known imaging parameters. Although  $\mathbf{A}$  can be expressed compactly above,  $\lambda_{eig}$  is more complex because the exponent N is usually greater than 20. Since  $\lambda$  describes the exponential evolution of the transient magnetization, it can also be written as  $\lambda_{image} = \exp(-T_{RR}/T_1^*)$ .  $T_1^*$  is determined from fitting the time point image data acquired during the transient phase (i.e., during the Look-Locker experiment). Because  $\lambda_{eig}$  is a function of two unknowns, the equation  $\lambda_{eig}(T_1, T_2) = \lambda_{image}$  can be solved for  $T_1$  and  $T_2$  by scanning twice with one parameter changed (e.g., flip angle).

Results A Bloch simulation of the pulse sequence in Figure 1 was performed, and  $T_1^*$  was determined by curve fitting.  $T_1$ ,  $T_2$ , and  $T_1^*$  were then calculated using  $\lambda_{eig}(T_1, T_2)$  and showed perfect agreement. An agarose gel phantom ( $T_1$ =2242 msec) was scanned using a ten-point bSSFP Look-Locker sequence. Imaging was performed twice with flip angles of 45° and 22.5°. A  $T_1^*$  value was determined for each of the two ten-image datasets, one for each flip angle. This produced two equations for  $\lambda_{eig} = \lambda_{image}$ . Solving these simultaneous equations yielded a  $T_1$  of 2367 msec.

**Discussion** Previously reported cardiac  $T_1$  mapping techniques using bSSFP have employed various assumptions and approximations to estimate  $T_1$ . This work presents an analytical expression for the transient phase of non-continuous-RF bSSFP. It provides the ability to directly quantify  $T_1$  for cardiac imaging while obviating any assumptions in acquisition or post-processing. Future work will involve continued evaluation on materials with a range of  $T_1$  and  $T_2$  values and the development of a single-breath-hold scan for clinical cardiac imaging. This method can also be used to calculate an optimal inversion time for magnetization-prepared scans based on imaging parameters.

References 1. Scheffler, MRM, 49:781 (2003). 2. Hargreaves, MRM, 46:149 (2001).