## Acceleration of multi-echo spin-echo imaging for T2 mapping using single or multiple coils

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Introduction: The measurement of  $T_2$  with a multi-echo spin-echo sequence is associated with a long acquisition time and a high SAR due to the use of a train of 180° RF pulses and a long TR [1]. Parallel acquisition techniques such as SENSE [2] or GRAPPA [3] allow a reduction of the number of phase encoding steps. However, their main limiting factor is, besides the number of available receive channels, the rapid decrease in SNR for higher acceleration factors. This work presents an alternative acceleration method that exploits the temporal correlation of the k-space signal at different echo times. It is based on a reconstruction algorithm that was presented in [4]. Here, an extension to the case of multiple coils is presented, and the approach is evaluated with respect to SNR and reconstruction artefacts.

**Theory**: The k-space sampling pattern proposed in [4] was implemented as shown in Fig. 1. Let R be the desired acceleration factor. Each spin-echo is straddled by its own phase-encoding and rewinder pair. During the echo train, the amplitude of the phase-encoding gradient is modified gradually to introduce a shift in k-space of  $\Delta k$ ,  $2\Delta k$ ... (R-1) $\Delta k$  between the first and the (R-1) consecutive echoes. After a cycle of R echoes, the gradient takes its initial value, and the next cycle starts. With that sub-sampling pattern, the number of phase-encoding steps is reduced by the factor R. The central part of k-space is acquired with full sampling for calibration purposes. The non-measured k-space data  $S_t(k)$  are then estimated by means of a linear combination of neighbors in the kt-space [4]:

$$\hat{S}_t(k) = \sum_{\tau=-n_t}^{n_t} \sum_{\kappa=-n_t}^{n_t} w_{\tau,\kappa} S_{t+\tau}(k+\kappa)$$
<sup>(1)</sup>

The coefficients w of the reconstruction kernel are estimated on the basis of the calibration samples. We now consider the case of signal acquisition with an array of N<sub>c</sub> coils. Since the relaxation process is Fig. 1: Modified multi-echo spin-echo sequence, with varying identical for all coil signals, the same kernel can be used to reconstruct each coil image separately.

Moreover, all coil calibration signals S<sup>cal</sup> can be included in the least-squares fit of the coefficients w:

$$\left(\hat{w}_{\tau,\kappa}\right) = \arg\min_{w} \sum_{\gamma=1}^{N_{\tau}} \sum_{t,k} \left( S_{\gamma,t}^{cal}\left(k\right) - \sum_{\tau=-n_{\tau}}^{n_{\tau}} \sum_{\kappa=-n_{k}}^{n_{k}} w_{\tau,\kappa} S_{\gamma,t+\tau}\left(k+\kappa\right) \right)^{2}$$
(2)

Thus, the reconstruction kernel reflects only the temporal correlation due to relaxation, and the estimation of its coefficients is improved by combining all coil signals. After Fourier transform, the reconstructed coil images can be described by the following expression:

$$\hat{s}_{\gamma,t}(x) = \sum_{u=0}^{R-1} s_t(x_u) c_{\gamma}(x_u) g_t(x, x_u) \quad \text{with } x_u = x + u \frac{FOV}{R}$$
(3)

 $c_{\gamma}$  is the coil sensitivity, and  $g_t$  models the kt-space reconstruction function in image space. Ideally,  $g_t(x,x_u)$ is a Dirac function, which is nonzero only if  $x=x_u$ . Since the kernel w has a limited number of coefficients,  $g_t(x,x_u)$  only approximates the Dirac function. Eq. (3) can then be inverted to yield an estimate of  $s_t(x)g_t(x,x)$ , which is a good approximation of the true signal  $s_t(x)$ . This inversion, as in SENSE, amounts to a multiplication with the sensitivity matrix  $(C^{H}C)^{-1}C^{H}$ .

Methods: Multi-echo spin-echo images for  $T_2$  mapping in the brain (32 echoes, 8ms echo spacing, resolution: 1.2×1.2×8mm, TR=1000ms) were acquired with a 6 channel head-coil on a 1.5T scanner (Achieva, Philips Medical Systems). Acceleration factors R of 2 and 4 were applied, with respectively 4

and 8 calibration phase-encoding steps. The same data were reconstructed with (a) SENSE, (b) GRAPPA, (c) the kt-reconstruction applied separately to each coil (denoted kt-T2), and (d) the multi-coil ktreconstruction (denoted MC kt-T2). GRAPPA and both kt-algorithms used the same calibration data. A reference scan was performed to measure the coil sensitivities required for SENSE and MC kt-T2. T<sub>2</sub> maps were computed by means of a non-linear least squares algorithm. Maps of the chi-square of the fit residuals were computed as an intrinsic measure of the reconstruction quality, since deviations from the exponential decay reflect both noise amplification and remaining folding artefacts.

Results and discussion: The mean normalized chi-squares of the fit residuals are listed in Tab. 1. Examples of  $T_2$  and chi-square maps for R=4 are shown in Fig. 2. Images and maps obtained with SENSE are characterized by significant noise amplification, while those obtained with GRAPPA (images not shown) suffer from folding artefacts, especially for R=4. Both kt-algorithms achieve superior reconstruction quality. Folding artefacts are almost completely removed with the multi-coil kt-T2 reconstruction. The kt-T2 methods make use of the redundancy in the multi-coil, multi-echo calibration signal to improve the estimation of the reconstruction kernel. This explains their better performance, as compared to GRAPPA, for the same number of calibration data.



gradient amplitudes, for R=2.

	(a) SENSE	(b) GRAPPA	(c) kt-T2	(d) MC kt-T2
R=2	0.0152	0.0143	0.0084	0.0075
R=4	0.0470	0.1421	0.0089	0.0080
Tab. 1: Mean normalized chi-squares of the fit residuals				

SENSE



Fig. 2:  $T_2$  and chi-square maps obtained with SENSE and the proposed multi-coil kt-T2 algorithm for R=4.

Conclusion: The linearity of the relaxation signals in kt-space forms the basis of the proposed kt-T2 method, which, like kt-BLAST and kt-SENSE [5], exploits the temporal correlation of the MR signal to reduce the number of encoding steps. Interestingly, for single coil acquisitions, this represents a new way of reducing the scan time that was not accessible with sensitivity encoding approaches. For multiple coils acquisitions, this extends the existing methods and allows an appreciable improvement in reconstruction quality, limiting especially noise amplification.

References: [1] Bernstein (2004). [2] Pruessmann et al, MRM, 42:952–962 (1999). [3] Griswold et al, MRM, 47:1202–1210 (2002). [4] Sénégas et al, ISMRM, #1785 (2007). [5] Tsao et al, MRM, 50:1031-1042 (2003).