

# Incorporation of a Vascular Term into a Reference Region Model for the Analysis of DCE-MRI Data

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**Introduction:** Dynamic contrast-enhanced MRI (DCE-MRI) can be used to characterize tumor physiology by tracking the movement of contrast between the vascular and extravascular spaces [1]. Models have recently been developed that allow for the analysis of DCE-MRI data without having to characterize the time course of the contrast agent concentration in the plasma—the so-called arterial input function (AIF) [2,3]. These “reference region” methods do not yet account for the plasma volume contribution, though several investigators have pointed out its significance in tumor studies [4,5]. In this work we explicitly incorporate a vascular term into the formalism and analyze, through simulations, its effect on the extracted pharmacokinetic parameters.

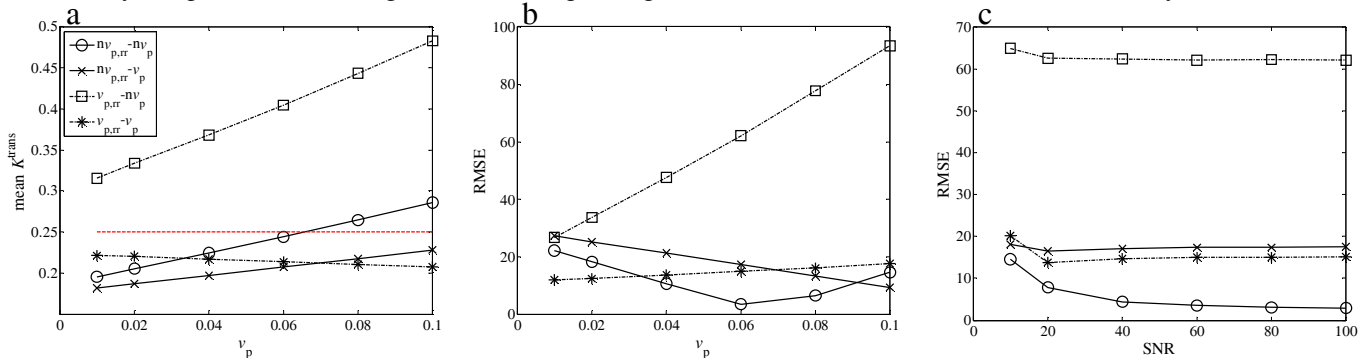
**Methods:** Simulations were run to calculate the transfer constant ( $K^{\text{trans}}$ ) and extravascular-extracellular volume ( $v_e$ ) using a reference region model [3] to examine the effects of the plasma volume fraction ( $v_p$ ). From the concentration time course in the reference region ( $C_{\text{RR}}$ ), plasma concentration ( $C_p$ ) may be calculated using Eq. 1 (excluding  $v_p$ ) or Eq. 2 (including  $v_p$ ).

$$C_p(t) = (1/K^{\text{trans,RR}}) \frac{d}{dt} C_{\text{RR}}(t) + (1/v_{e,\text{RR}}) C_{\text{RR}}(t) \quad (1) \quad C_p(t) = \frac{1}{v_{p,\text{RR}}} \int_0^t \frac{dC_{\text{RR}}}{dt}(u) e^{-K^{\text{trans,RR}} \left( \frac{1}{v_{p,\text{RR}}} + \frac{1}{v_{e,\text{RR}}} \right) (t-u)} du + \frac{K^{\text{trans,RR}}}{v_{p,\text{RR}} v_{e,\text{RR}}} \int_0^t C_{\text{RR}}(u) e^{-K^{\text{trans}} \left( \frac{1}{v_{p,\text{RR}}} + \frac{1}{v_{e,\text{RR}}} \right) (t-u)} du \quad (2)$$

A plasma curve was generated using parameters previously described [6], with a time step of 1 sec. In the reference region, tissue curves were generated using  $K^{\text{trans}} = 0.08 \text{ min}^{-1}$ ,  $v_e = 0.1$ , and  $v_p = 0.02$ . In the tissue of interest,  $K^{\text{trans}} = 0.25 \text{ min}^{-1}$ ,  $v_e = 0.4$ , and  $v_p = 0.01 - 0.1$ . Noise was added to the tissue curves so that the SNR (relative to the peak reference region concentration) varied from 10 to 100, and they were sampled at an interval of 15 sec. The plasma signal was calculated using Eq. 1 or Eq. 2. This plasma signal was then used to calculate kinetic parameters in the tissue of interest, either excluding or including the vascular signal. A series of 1000 Monte Carlo runs were performed, and the mean and percent root mean square error (RMSE) in the kinetic parameters was calculated.

**Results:** The mean value of  $K^{\text{trans}}$  vs.  $v_p$  is shown in Fig. 1a (SNR=60). The actual value of  $K^{\text{trans}}$  (0.25) is shown by the dashed red line. If  $v_p$  was excluded from both regions ( $nv_{p,\text{rr}}-nv_p$ ),  $K^{\text{trans}}$  was underestimated for  $v_p < 0.06$  and overestimated for  $v_p > 0.06$ . If  $v_p$  was excluded from the reference region and included in the tissue of interest ( $nv_{p,\text{rr}}-v_p$ ),  $K^{\text{trans}}$  increased with  $v_p$ , but was less than the true value. If  $v_p$  was included in the reference region and excluded from the tissue of interest ( $v_{p,\text{rr}}-nv_p$ ),  $K^{\text{trans}}$  was overestimated by an amount that increased linearly with  $v_p$ . If  $v_p$  was included in both regions ( $v_{p,\text{rr}}-v_p$ ),  $K^{\text{trans}}$  was slightly underestimated. Fig. 1b plots RMSE vs.  $v_p$  (SNR=60). For the  $nv_{p,\text{rr}}-nv_p$  case, the RMSE decreased almost to zero and then increased with increasing values of  $v_p$ . For the  $nv_{p,\text{rr}}-v_p$  case, the RMSE decreased linearly with  $v_p$ . For the  $v_{p,\text{rr}}-nv_p$  case the error increased linearly with  $v_p$ . The error remained relatively stable for the  $v_{p,\text{rr}}-v_p$  case. The SNR sensitivity of the  $K^{\text{trans}}$  RMSE is shown in Fig. 1c ( $v_p=0.06$ ). If  $v_p$  was excluded from both regions, then the error in  $K^{\text{trans}}$  decreased with increasing SNR, from 15% to 3%. For all other cases, the errors were relatively stable for SNR > 20, and were 17% ( $nv_{p,\text{rr}}-v_p$ ), 62% ( $v_{p,\text{rr}}-nv_p$ ), and 15% ( $v_{p,\text{rr}}-v_p$ ). The trends for  $v_e$  were similar to  $K^{\text{trans}}$  in both the effects of increasing  $v_p$  and SNR (data not shown).

**Conclusions:** The importance of the plasma term in calculating  $K^{\text{trans}}$  and  $v_e$  from the reference region model were analyzed. If the  $v_p$  term was included in both regions, this resulted in an RMSE of 10-15% for the range of  $v_p$  and SNR studied. If the  $v_p$  is not known in the reference region, then it should also be excluded from the tissue of interest calculations. The largest errors resulted if the vascular term was included in the reference region and excluded from the tissue of interest. These findings are consistent with previous AIF driven DCE-MRI analyses in which the effects of a vascular term were investigated [7]. Planned studies will apply these methods *in vivo* to directly compare a reference region model incorporating the vascular term to that of a standard AIF analysis.



**Figure 1:** (a) Mean  $K^{\text{trans}}$  vs.  $v_p$  (SNR=60). True value of  $K^{\text{trans}}$  (0.25) is shown by the red dashed line. (b) Error in  $K^{\text{trans}}$  vs.  $v_p$  (SNR=60). (c) Error in  $K^{\text{trans}}$  vs. SNR ( $v_p=0.06$ ).

**References:** [1] Tofts PS, et al. J Magn Reson Imaging. 1999; 10:223-232. [2] Kovar DA, et al. J Magn Reson Imaging. 1998; 8:1126-1134. [3] Yankeelov TE, et al. Magn Reson Imaging. 2005; 23:512-529. [4] Harrer JU, et al. J Magn Reson Imaging. 2004; 20:748-757. [5] Henderson E, et al. J Magn Reson Imaging. 2000; 12:991-1003. [6] Parker GJM, et al. Magn Reson Med. 2006; 56:993-1000. [7] Buckley DL. Magn Reson Med. 2002; 47:601-606.