

Assessment of Dynamic Averaging From Transverse Relaxation in the Rotating Frame (T_{2p}) During Adiabatic HS n Pulses.

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Introduction

Conventional techniques used to access dynamic averaging (DA) include Carr-Purcell spin echo (SE) and on/off-resonance $T_{1\rho}$ methods. T_{2p} relaxation has not been investigated probably because of the experimental difficulties associated with measuring T_{2p} . During the application of the adiabatic pulses, the time-dependent effective field $\omega_{\text{eff}}(\mathbf{t})$ affects the $T_{2p}(t)$ by changing the axis of quantization. During the pulses in the adiabatic CP sequence known as CP-LASER (1,2), magnetization precesses in the plane approximately perpendicular to $\omega_{\text{eff}}(\mathbf{t})$ (2); thus the time-dependent transverse relaxation in the double rotating frame (TDRF) is mainly responsible for the MR signal decay. This work was focused on the time-dependent Hamiltonian $H=h/(2\pi)E(I,t)$ case, e.g. the interaction energy of the nuclear magnetic moments with the time-dependent externally applied magnetic field. This approach includes dipolar relaxation and DA (during the adiabatic pulse) components, as represented by the following Eq: $R_2^\ddagger = R_{2p}^{dd}(t) + R_{2p}^{DA}(t)$. In this work water-glycerol samples with high viscosity (30%/70% by volume), as well as the cerebral metabolite Creatine/Phosphocreatine (tCr, 3.03 ppm) in human brain were investigated as a function of the τ_{cp} (interpulse time interval of the CP-LASER sequence) with HS1 and HS4 pulses.

Methods

Transverse relaxation times of water in glycerol (30%/70%) were measured at 4.7T using localized spectroscopy based on the CP-LASER technique. TE of the sequence was incremented by increasing of the number of HS n pulses in the CP-train. The CP-train was composed of 3-ms-long HS n ($n=1$ or 4) pulses with an adiabaticity factor R of $AT_p/20$ (pulses length $T_p=0.003$ s), using various delays between pulses. The modulation functions of HS n pulses differ with the choice of n . Three different RF amplitudes ($\omega_1^{\text{max}}=2.5, 5, 10$ kHz) were used for the T_2^\ddagger measurements of water in glycerol. T_2^\ddagger of brain tCr were also measured at 7T. Four healthy volunteers participated in the studies. Interleaved acquisitions were performed with the HS1 and HS4 pulses (R=20) in the CP-train as a function of τ_{cp} .

Results and Discussion

During the adiabatic pulses the magnetization undergoes precession around the rotating $\omega_{\text{eff}}(\mathbf{t})$ and remains approximately perpendicular to $\omega_{\text{eff}}(\mathbf{t})$ when the adiabatic condition is satisfied. Transverse dipolar relaxations of a system of two equivalent nuclei of a spin I in the TDRF were considered by Blicharski (3). Under the experimental conditions of $\omega_0 \gg \omega_{\text{eff}}$, one obtains:

$$1/T_{2p}^{dd}(t) = 1/(40 k_{dd}) [3 \cos^2 \theta - 1]^2 + 30 \sin^2 \theta \cos^2 \theta J(\omega_{\text{eff}}(t)) + 3 \sin^4 \theta J(4 \omega_{\text{eff}}(t)) + (20 - 6 \sin^2 \theta) J(\omega_1) + (8 + 12 \sin^2 \theta) J(4 \omega_{\text{eff}}(t)) \quad (1)$$

where $1/k_{dd} = (h/(2\pi))^2 2I(I+1) \gamma^4 r^{-6}$, r is the inter nuclear distance, $h/(2\pi)$ is the Planck's constant, γ is the gyromagnetic ratio of the protons, and τ_c is the rotational correlation time. Integration over the pulse length was performed to calculate the averaged relaxation time: $T_{2p} = 1/T_p \int_0^{T_p} T_{2p}(t) dt$. We found that the DA contribution during the pulse can be described by the Eq.2: $R_2^{DA} \sim F(\vartheta) \Delta\omega k^{DA} / (k^{DA} + B(\omega_{\text{eff}}(t)))$, where $B(\omega_{\text{eff}}(t))$ and $F(\vartheta)$ are the time dependent functions, that are specific to the adiabatic pulse used. The relaxation rate during the interpulse time intervals is presented by the following Eq. 3: $1/T_2^\ddagger = ((R_{2p}^{dd}(t) + R_{2p}^{DA}(t)) - 1/T_2) T_p / \tau_{cp} + 1/T_2$, where the contribution of DA as a function of the delay time can be described by the general model for the DA (4): $1/T_2 = \Delta\omega^2 \tau_{cp} \alpha \beta x \{1 - b x \tanh [1/(bx)]\}$; $x = \tau_{d,ex} / \tau_{cp}$; $\tau_d = r^2/D$. Here D is apparent diffusion coefficient, $\tau_{d,ex}$ is the correlation time for diffusion or exchange and $\Delta\omega$ is the chemical shift difference between exchangeable protons or background susceptibility gradients.

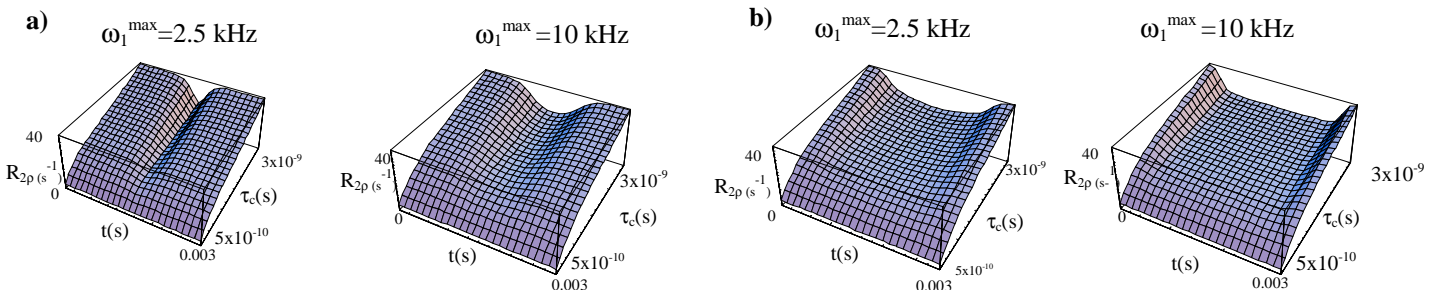


Figure 1 Calculated transverse relaxation rates (R_{2p}^{dd}) in the TDRF during the a) HS1 and b) HS4 pulses as a function of the rotational correlation time (τ_c) and time during the pulse. The pulse parameters used for calculation were: pulse length $T_p=0.003$ s, R=20, $\omega_1=2.5$ kHz.

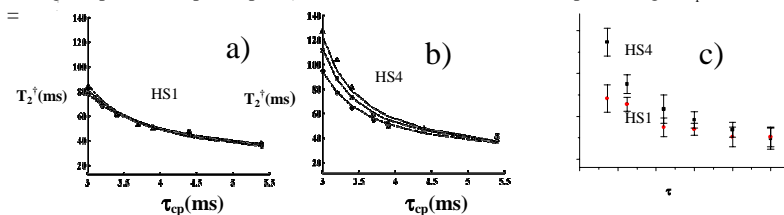


Figure 2. (a) T_2^\ddagger measurements of water in glycerol as a function of the τ_{cp} and the ω_1^{max} with HS1 pulse; (b) same as (a), but using HS4 pulses in the CP-train of CP-LASER. The superimposed dashed lines are the theoretical simulations according to Eq. (3). The results of the simulations are: $\tau_c=1.12 \times 10^{-10}$ s, $\tau_{\text{ex}}=0.1$ ms; (c) T_2^\ddagger measurements of tCr as a function of τ_{cp} .

There was no significant difference between T_2^\ddagger measured with HS1 pulses using ω_1^{max} 2.5 kHz or 10 kHz. On the other hand, T_2^\ddagger s measured with the HS4 pulses exhibited significant increase when ω_1^{max} increased. Analysis of the experimental data indicate that the dominant contribution to the MR signal decay in CP-LASER is DA, and during the pulse is governed mainly by the time-dependent $T_{2p}^{DA}(t)$ term. This approach provides the possibility to assess MRI contrast based on DA. The contribution of the time-dependent $T_{1\rho}(t)$ was neglected due to the fact that the magnetization precesses in the plane perpendicular to $\omega_{\text{eff}}(\mathbf{t})$. The time-dependent T_{2p} relaxation process also provides sensitivity to dipolar interactions of the slow moving spins ($\tau_c > 5 \times 10^{-9}$ s). In such cases, interleaved measurements of T_2^\ddagger s using adiabatic pulses with the different modulation functions may be used to determine the rotational and diffusion/exchange correlation times of the spins of interest.

References 1), Michaeli et. al, MRM, **47**, 2002, p. 629; 2) Garwood et. al, JMR, **153**, 2002, p155; 3) Blicharski, Acta Physica Polonica, 1971, **A41**, p 223; 4) R. Brooks, et al., MRM **45**, 1014-1029 (2001).

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