

# Computational comparison of two RF coil configurations for SENSE imaging

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**Synopsis.** The ultimate factor  $g$  was used to theoretically compare performance of two coil geometries for SENSE imaging. The circular SNR formula based on the quasi-static model was used, and the PERES coil SNR was calculated following the same approach. These expressions together with the ultimate factor  $g$  formula were used to compute ultimate-factor- $g$ -vs-distance plots for comparison purposes. The PERES coil factor  $g$  can be up to 27% below that of a single circular-shaped coil. This improvement makes PERES coil a good choice for SENSE imaging. The present method strengthens the  $g$  simulation approach to evaluate coil performance for SENSE applications.

**Introduction.** The SENSE technique exploits the spatial information generated by receiver coil array coils for signal localisation in order to reduce gradient encoding. Image noise is enhanced locally as a result of reduced gradient encoding when the used coil array does not provide ideally distinct spatial sensitivities. This effect usually becomes relevant for reductions larger than a factor of two. It can be quantitatively described by the so-called geometry factor  $g$ . In addition to conventional array development considerations the geometry factor  $g$  must be taken into account. Although  $g$  is difficult to estimate intuitively, it has been found that relatively basic simulations can give a good forecast of the performance of a certain array configuration. In this research, the *ultimate factor*  $g$  proposed by [1] is used to compare the coil performance of a circular-shaped coil and the PERES coil [2] for SENSE imaging.

**Method.** Reykowski [1] has recently calculated an analytical expression for the ultimate factor  $g$  for 2 ideal coils:

$$g^{ultimate} = \frac{SNR^{full}}{SNR^{SENSE}} = \left( 1 - \frac{S_{12}^2}{S_{11}^2} \right)^{-\frac{1}{2}} \quad [1]$$

where  $S_{11}$  and  $S_{12}$  are the SNR of coils 1 and 2 at point 1 respectively. Eq. [1] shows that the ultimate factor  $g$  depends on the coil SNR. To compare the coil performance of these two coil design, the quasi-static model described in [3] was used to calculate a mathematical formula for the SNR of PERES coil (Eq. [2]), and the single-loop coil SNR (Eq. [3]) was also obtained from [3]:

$$SNR_{PERES} = \frac{MV \cos(\omega)}{\sqrt{(kT \Delta f \sigma)}} \sqrt{\frac{3N}{16l(b_{PERES}^2 + d^2)^3}} \quad [2], \quad SNR_{cir} = \frac{MV \sqrt{b_{cir}}}{\sqrt{(b_{cir}^2 + d^2)^3}} \sqrt{\frac{3}{16kT \sigma \Delta f}} \quad [3]$$

where  $M$  is the magnetisation density,  $V$  is the voxel volume,  $b_{cir}$  is the circular coil radius,  $d$  is the depth at a given point  $p$ ,  $\Delta f$  is the bandwidth of the receiver low-pass filter,  $k$  is the Boltzmann constant,  $\sigma$  is the conductivity of half-space, and  $T$  is the temperature of the loss resistance. In Eq. [2],  $\omega$  is the angle representing the centre of the coil of radius  $a_{petal}$  (petal coil radius) relative to the coil of radius  $b_{PERES}$  (total radius),  $l a_{petal} = b_{PERES}$  (total radius), and  $N =$  number of petal coils. MatLab (V. 6.1, The MathWorks, Natick, MA) programmes were specially written to calculate the ultimate factor  $g$  profiles for these two RF surface coils. To assess the performance of these coils, ultimate  $g$  expressions were calculated for both coil configurations by substituting Eqs. [2] and [3] in Eq. [1] with  $\omega = 0$  for the case of two points as shown in Fig. 1.

**Results and Discussion.** The  $g$  profiles of the two coils were computed with reduction factor  $R = 1$ ,  $b_{PERES} = b_{cir} = 10$  cm, and the following parameters,  $d$  (coil 1):  $0 < d < 10$  and  $d_{pha} - d$  (coil 2):  $0 < d_{pha} - d < 10$ .  $g$ -vs- $d$  plots were then obtained and shown in Fig. 2(left). To evaluate coil performance an improvement plot was also estimated and shown in Fig. 2(right). It can be appreciated from Fig. 2 (left) that the factor  $g$  of the PERES coil shows a considerable improvement over the single-coil profile. Results of Fig. 2 (right) indicate that there is no evident change for the factor  $g$  for points near the surface coil (Coil 1 or Coil 2) according to the layout of Fig. 1, and that the upper limit of PERES coil factor  $g$  is about 27% below the factor  $g$  of the circular coil for distant points. An important limitation is that a coil SNR expression is required. To find an analytical expression for the SNR is a difficult task since coil designs can take very complicated configurations. These results are in good agreement with those reported in [4]. The PERES design shows better performance than the circular coil for SENSE imaging applications. Unlike the computationally-demanding and time-consuming simulations, the ultimate factor  $g$  expression offers a straightforward way to predict coil performance for SENSE techniques.

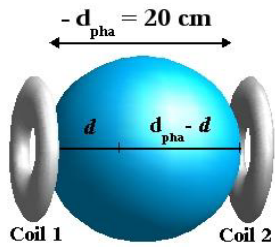


Figure 1. Two points along the diameter in a lossy half space for the quasi-static model.

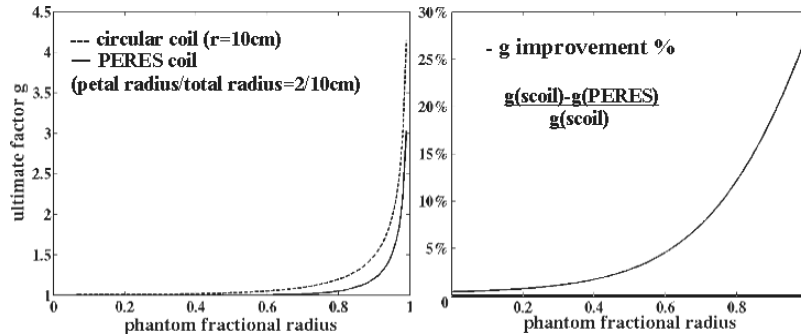


Figure 2. Left) The lower  $g$  profiles of PERES coil shows improvement coil over the circular coil. Right) Improvement profile shows the 27% upper limit.

## References

1. Proc 10 ISMRM, p. 905, 2002.
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